

# Collisional excitation of interstellar molecules: towards reactive systems

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de France**

## Context

- *Astrochemistry*: obtaining the **most accurate census of the molecular content** in the interstellar medium (ISM)

*Key questions:* *How do stars and planets form?*

*How do the organic molecules form?*

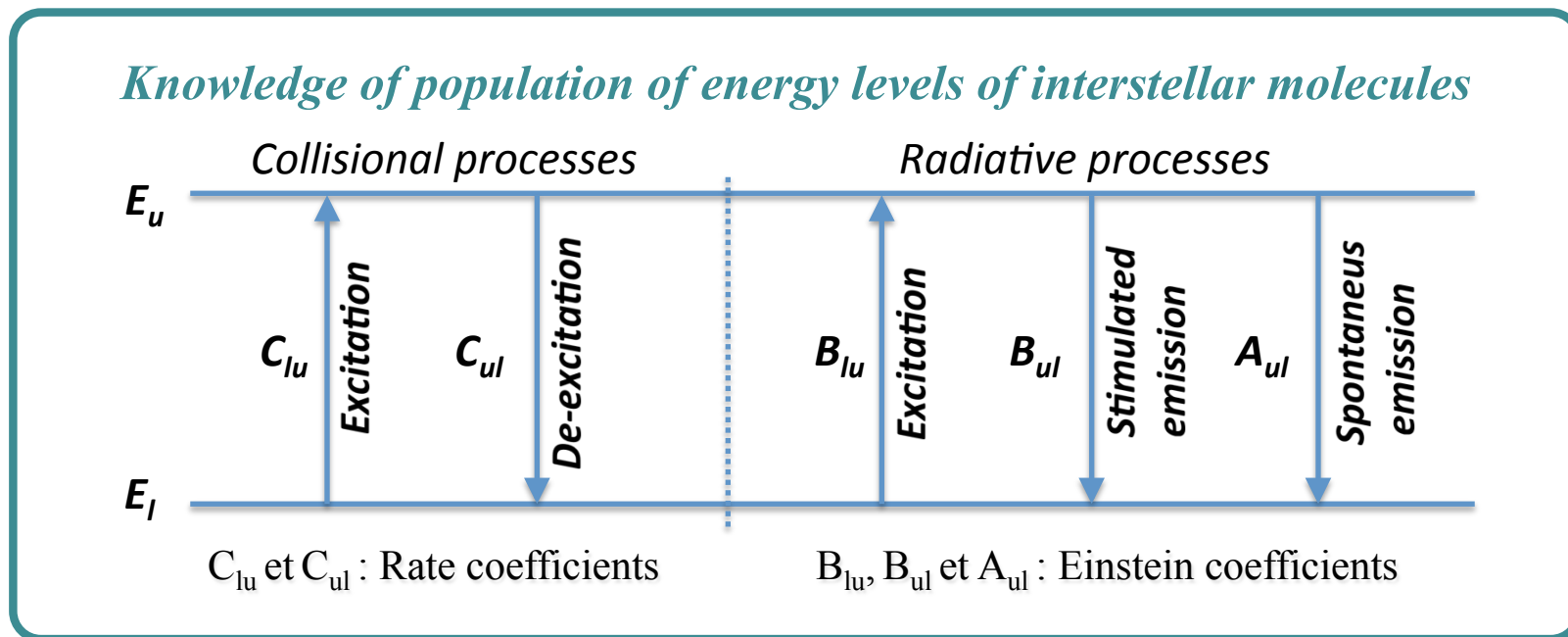
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Key questions: *How do stars and planets form?*

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- Our knowledge about ISM relies on **molecular spectra**
- In the ISM, the low density cannot maintain local thermodynamic equilibrium (LTE)
- **Non-LTE analysis** of the observational spectra is required



**Studying collisional excitation of interstellar molecules by H and H<sub>2</sub>**

## What has been done so far?

- Excitation studies of interstellar molecules **began in the 70's** (Dalgarno, Green, Flower,...)
- “**Molecular Universe**” RTN network (2004-2008): update for a number of key molecules
- Full **quantum calculations** feasible
- Theoretical calculations **rival the accuracy of experimental data**
- **Highly accurate data available** for ~50 molecules (over ~300 detected)
- **Precise determination of the molecular content** in molecular clouds

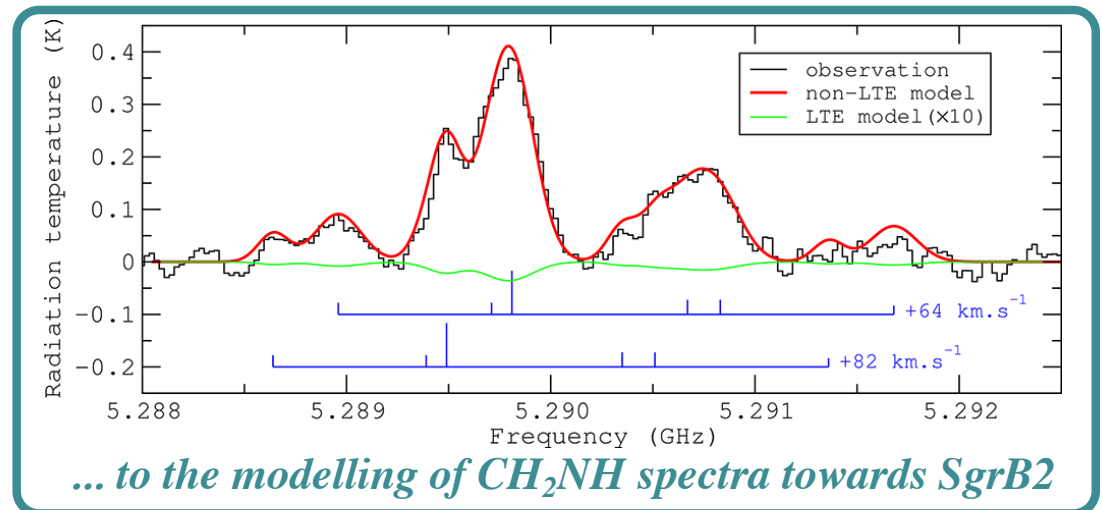
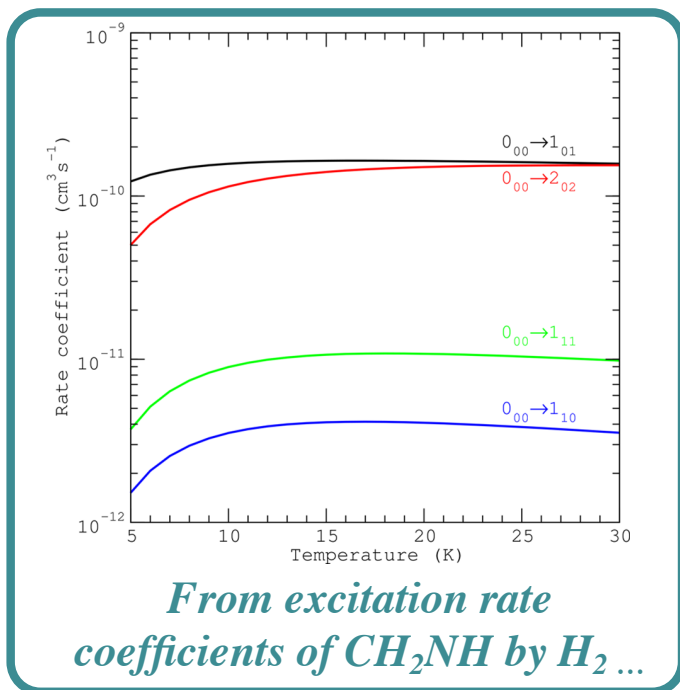
*See the review by Roueff and Lique (2013)*



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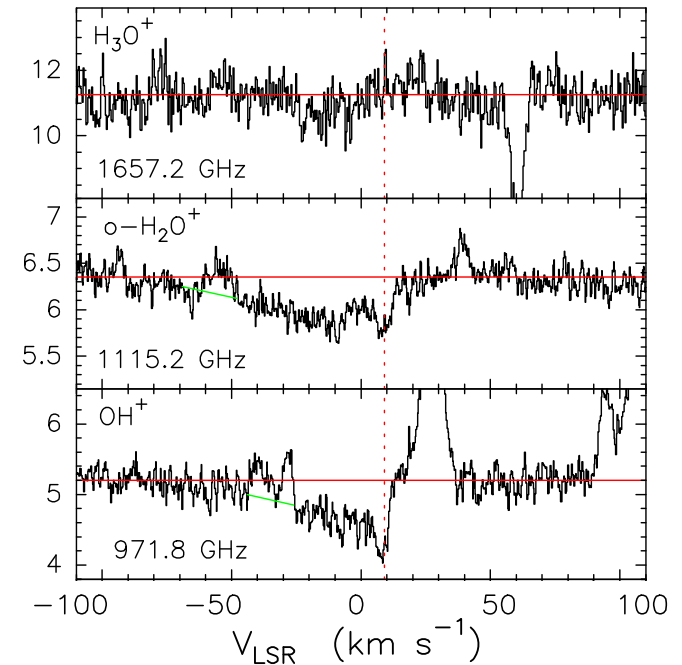
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*Faure, Lique and Remijan (2018)*

## Detection of new (reactive) molecules

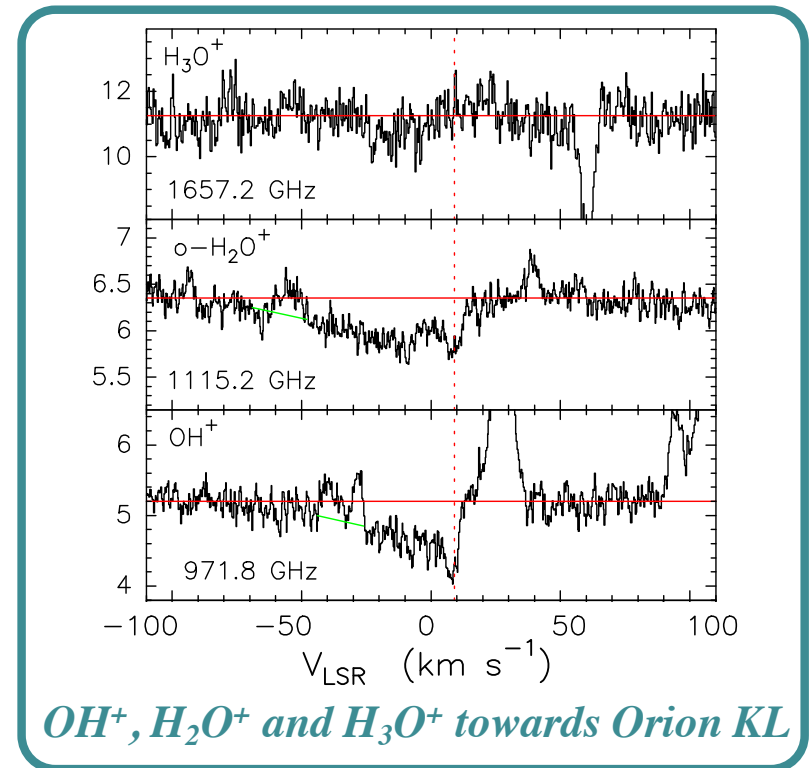
- New telescopes allow **highly resolved observations**
- Detection of **reactive molecules** ( $\text{H}_2\text{O}^+$ ,  $\text{OH}^+$ , CH HS...), i.e. **rapidly destroyed** by H,  $\text{H}_2$  or  $e^-$  (Black 1998)
- **Key species** for astrochemistry
- Accurate analysis of the spectra is **hampered by the complete lack of collisional data**



*$\text{OH}^+$ ,  $\text{H}_2\text{O}^+$  and  $\text{H}_3\text{O}^+$  towards Orion KL*

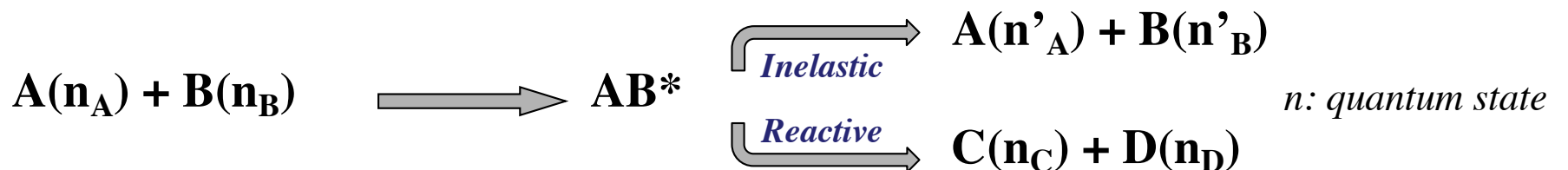
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Problematic: *How can we get such collisional data?*

- Complex competition between inelastic and reactive processes



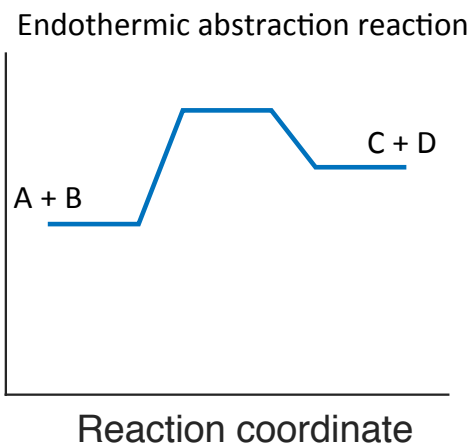
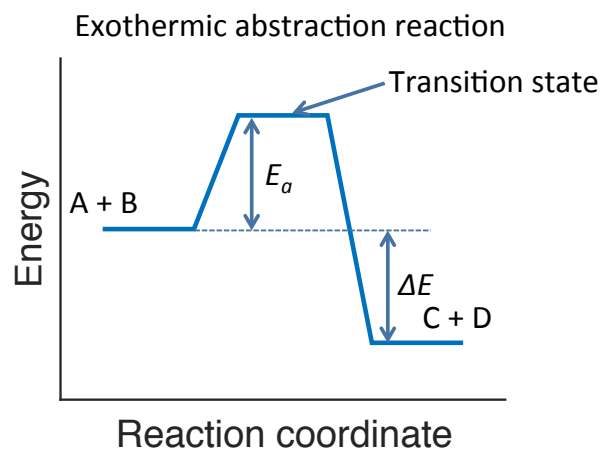
- **No available methods and codes** to take into account the reactivity at a **state-to-state level**

**Development of new methods to provide collisional data for these molecules**

## Towards a method to fully consider the inelastic / reactive competition

Schematically, the dynamics of gas-phase reactive collisions are governed by two mechanisms:

### *Abstraction reaction:*

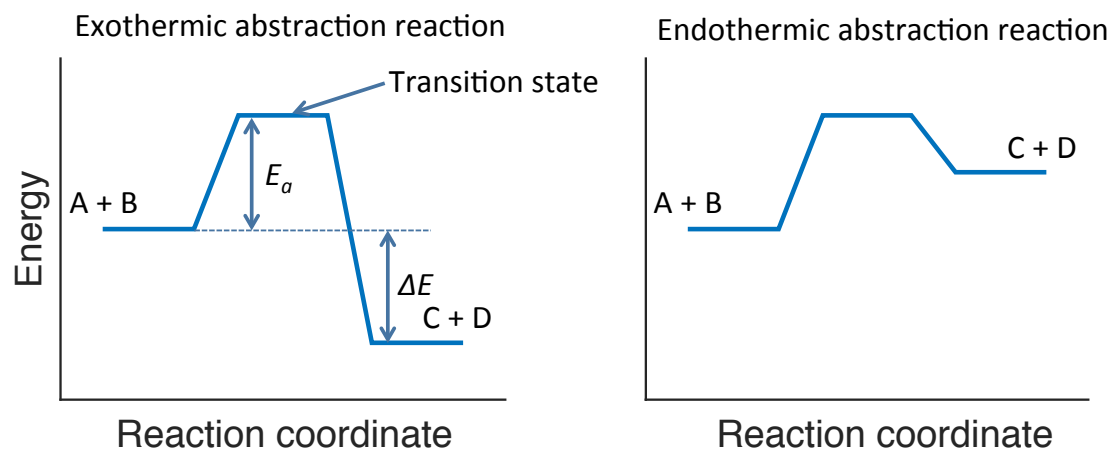


- **Reduced dimension approaches** (neglecting the reaction process) may be reliable at ISM temperatures
- **Validity domain (if any) and accuracy** of these approaches

## Towards a method to fully consider the inelastic / reactive competition

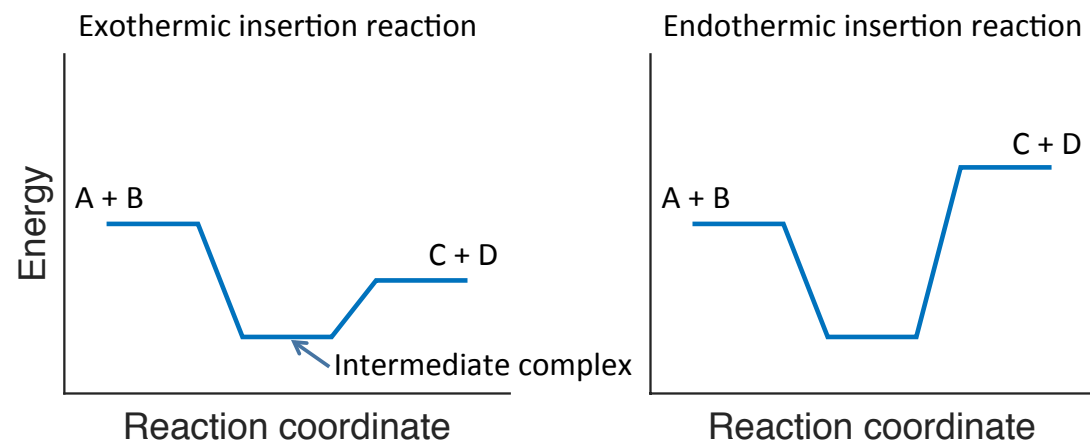
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### Insertion reaction:



- **Reactive channels need a priori to be included** (especially for exothermic reactions)
- **Statistical quantum approaches\*** can be used to generate accurate data for both collisional excitation and reactive processes

\* *Formation of a long-lived intermediate complex: statistical distribution of the population of the energy levels*

# Study of molecular systems

## Born-oppenheimer approximation (1927)



2 stages :

*ab initio* calculation of the potential energy surface between particles

**Quantum chemistry**  
Semi-empirical methods

Study of the dynamical of the nuclei

**Quantum Methods (TI et TD)**  
**(Quasi-)Classical methods**  
**Statistical methods**

*Collisional cross sections calculations:*

Accuracy ↓

- **Close Coupling** (CPU time = Channel number<sup>3</sup>)
- **Coupled states** (Neglect centrifugal distorsion)
- **Quasi-Classical Trajectory**

↑ - **Statistical methods ?**

# Reduced dimension approaches

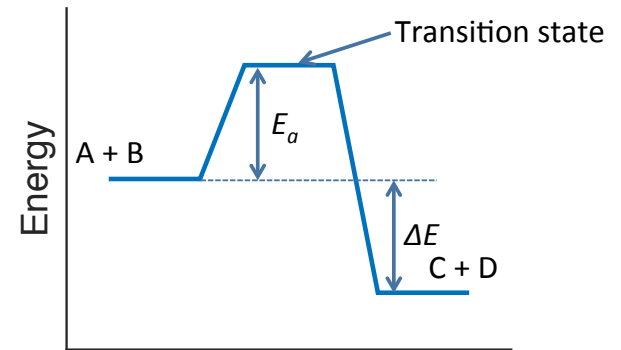
## Methods:

- Target: **rigid rotor** (internuclear distance fixed)
- **Reactive channels are closed**
- Equivalent to pure inelastic scattering

## Questions:

- **Validity domain and accuracy**
- Strategy for computing the interaction potential

## *Abstraction reaction:*



# Reduced dimension approaches

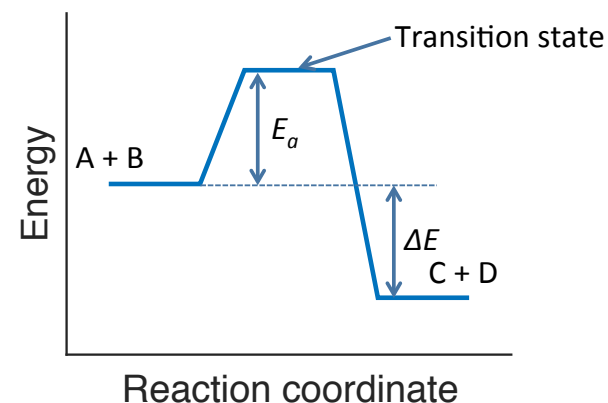
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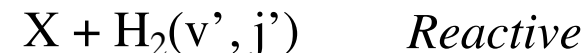
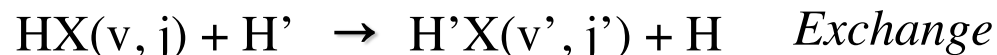
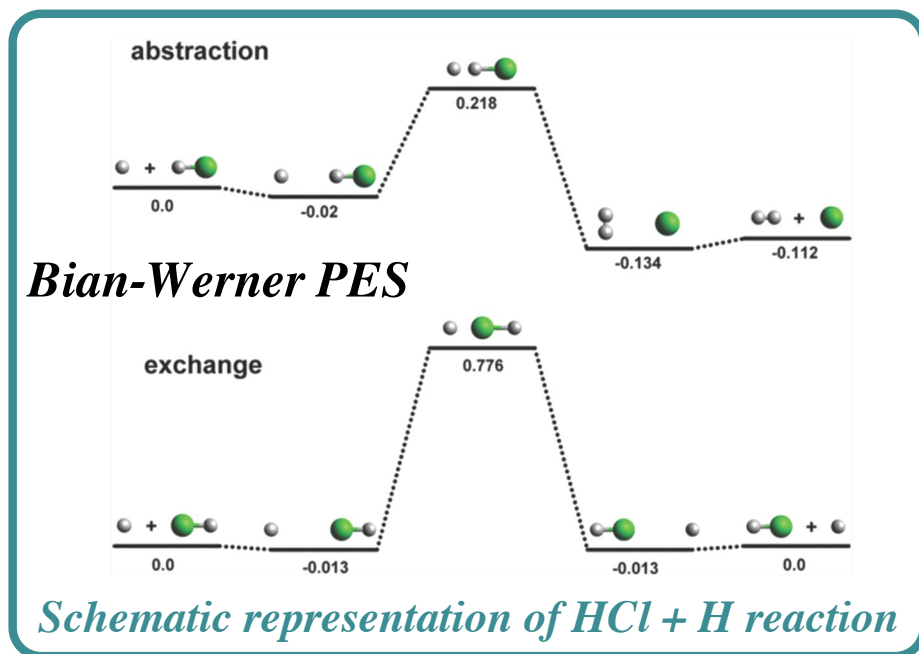
## Questions:

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### Abstraction reaction:



## Rigid rotor vs. Reactive calculations



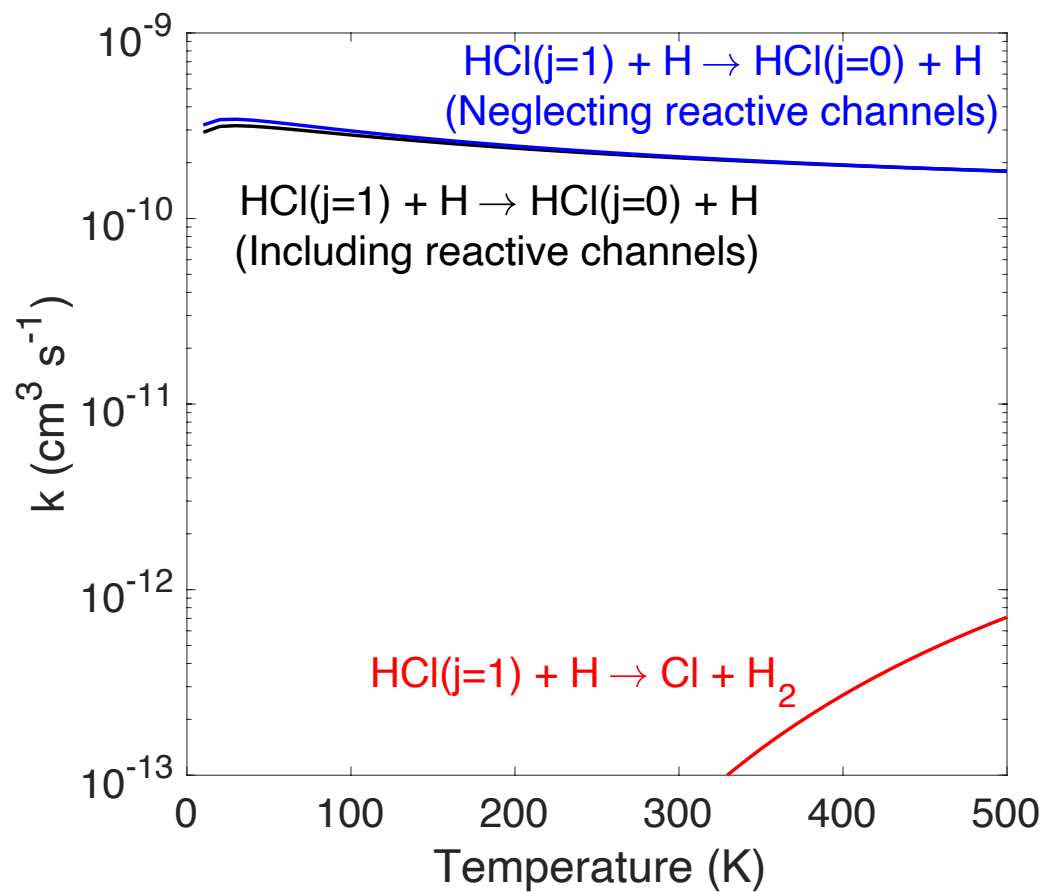
Reactive channels are endo/exothermic

**Influence of the reactive channels ?**  
*(Reactive and exchange channels are inhibited by a large barrier)*



## Reduced dimension approaches: HCl-H

### Inelastic vs. reactive approaches for the excitation of HCl by H

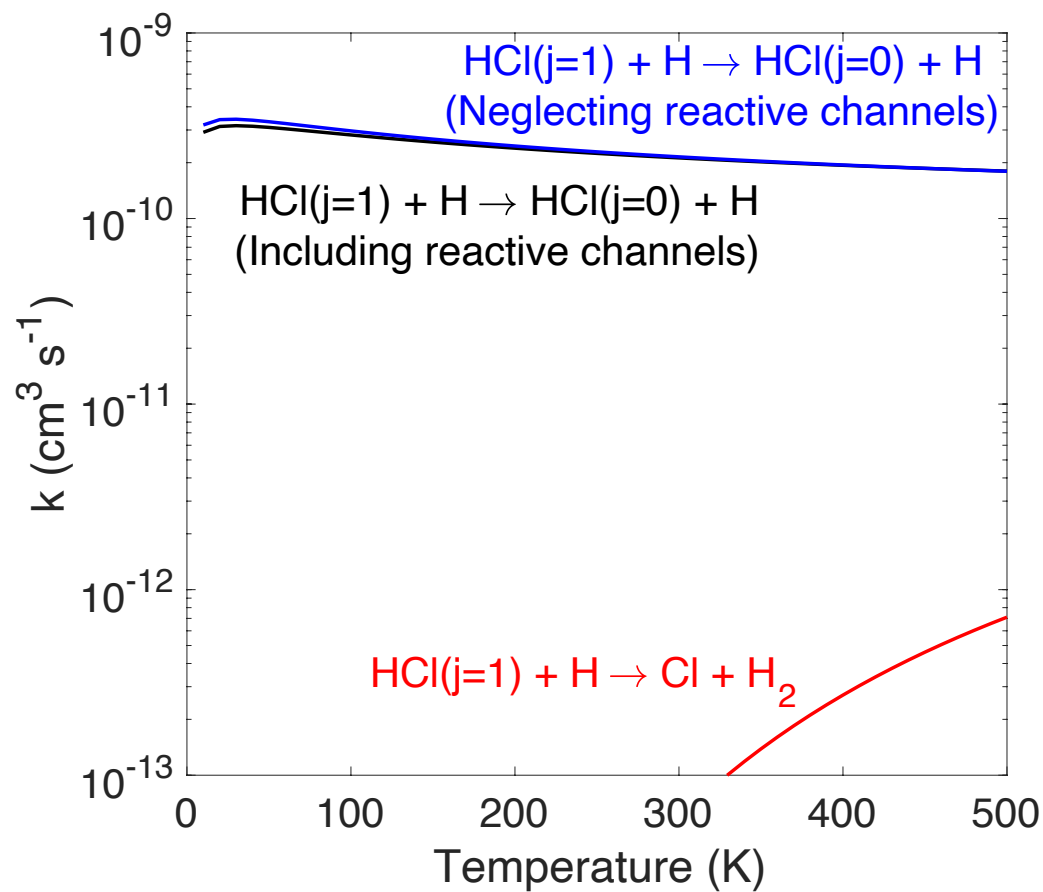


*Rotational relaxation and destruction of HCl(j=1) induced by collisions with H*

- Accurate description of the rotational excitation obtained using the rigid rotor approach

## Reduced dimension approaches: HCl-H

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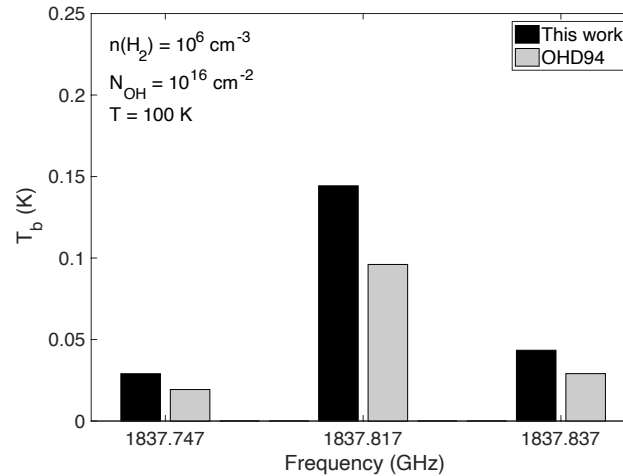
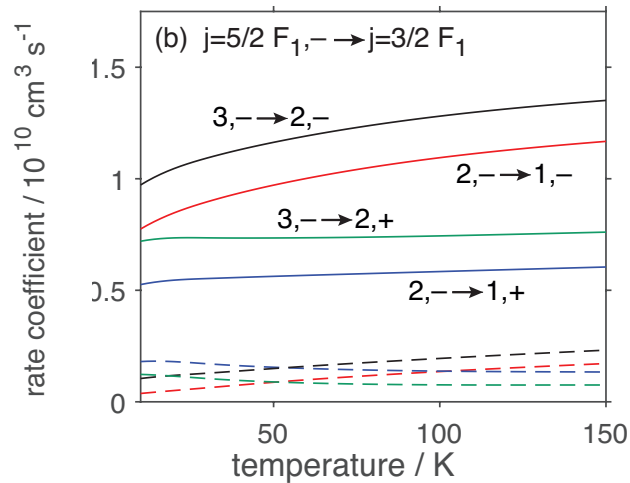
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**Validation of rigid rotor approaches for reactive systems with barrier**

# Reduced dimension approaches: Applications

## Collisional excitation of OH by H<sub>2</sub>

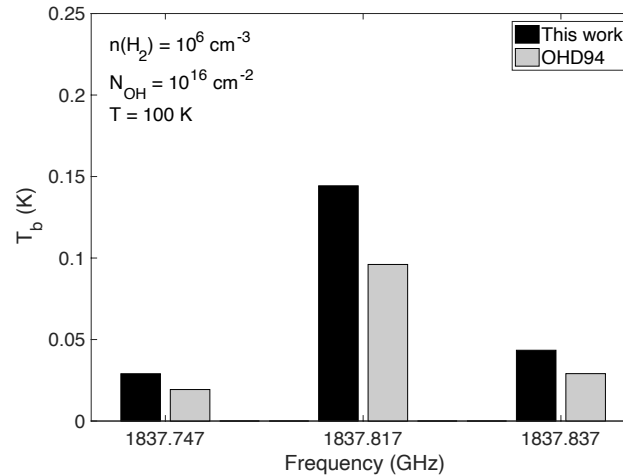
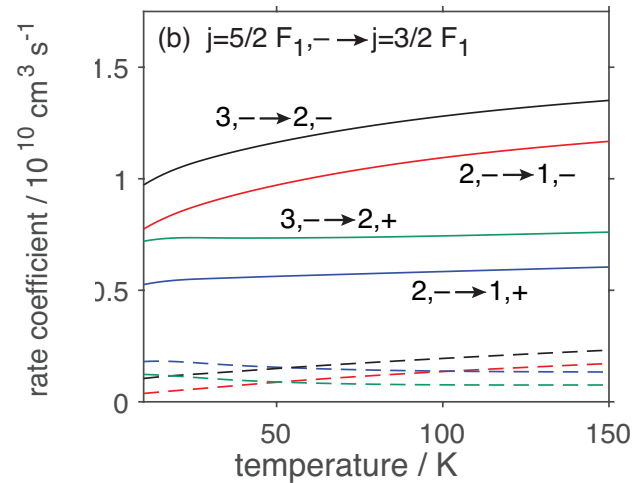


**The new rate coefficients increase the line intensities by a factor ~1-2**

*OH-H<sub>2</sub> Hyperfine resolved rate coefficients and brightness temperature of some OH lines obtained with present and previous Offer et al. (1994) rate coefficients*

# Reduced dimension approaches: Applications

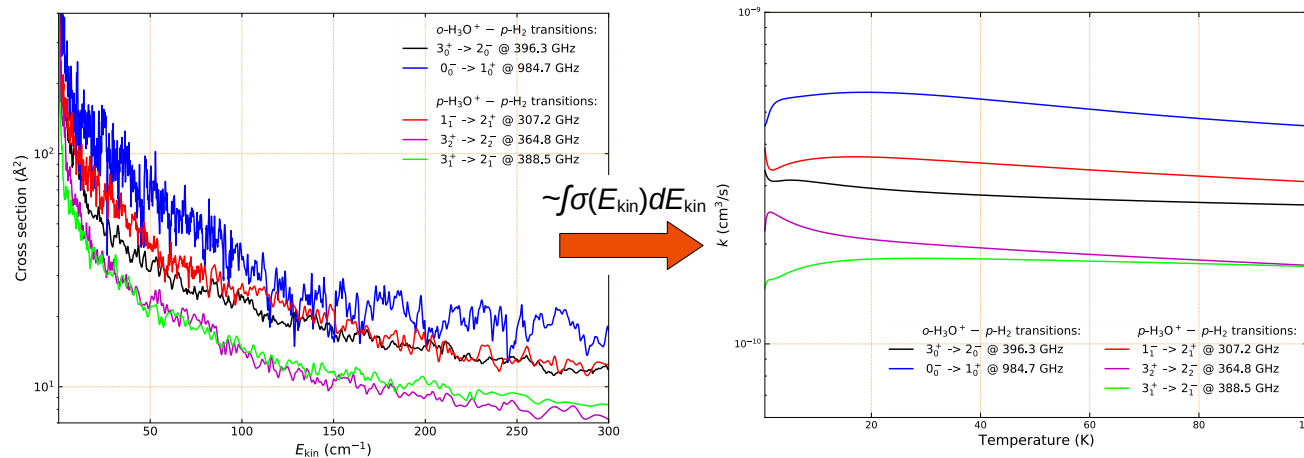
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## Collisional excitation of H<sub>3</sub>O<sup>+</sup> by H<sub>2</sub>

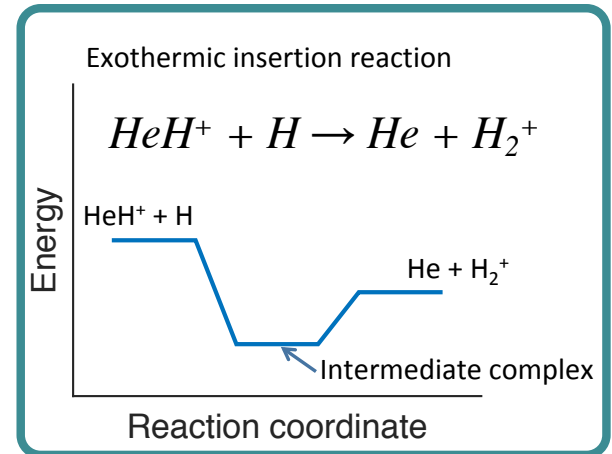
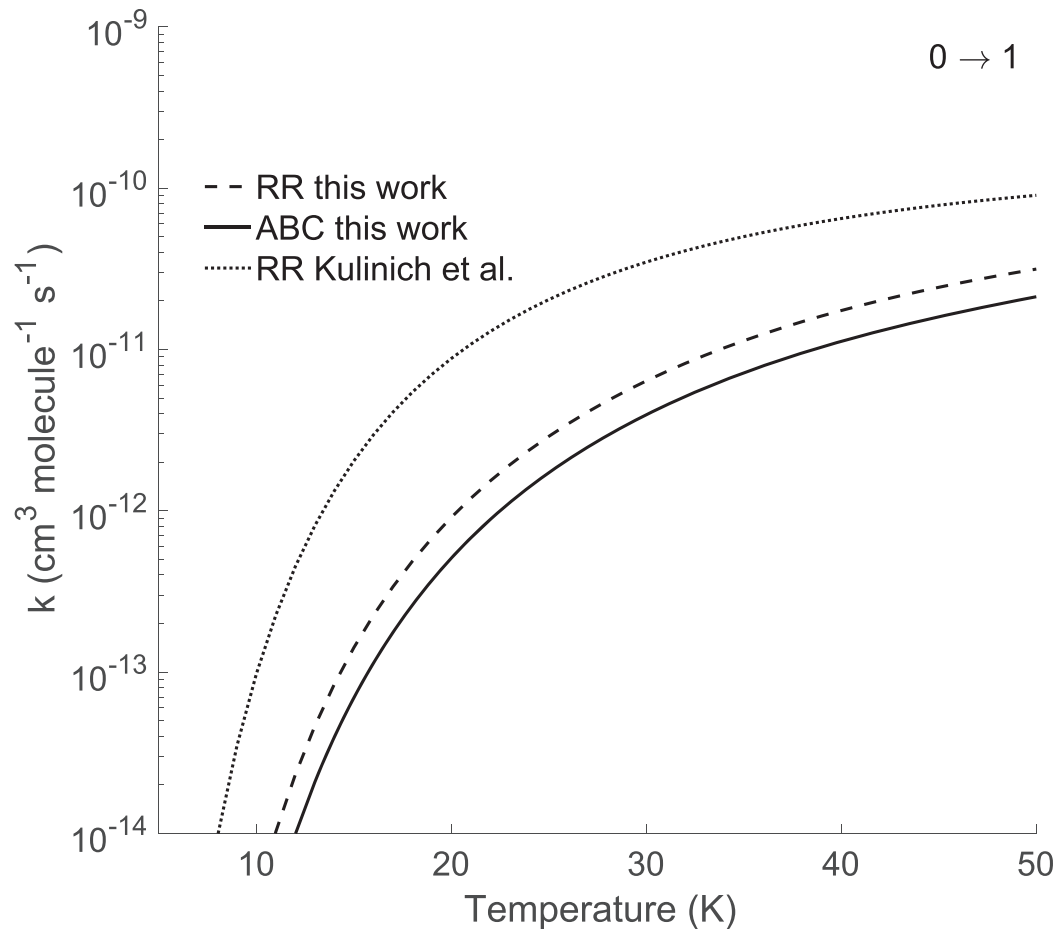


First state-to-state rate coefficients for the H<sub>3</sub>O<sup>+</sup>-H<sub>2</sub> collisional system

*Cross sections and rate coefficients for transitions in H<sub>3</sub>O<sup>+</sup> induced by H<sub>2</sub>(j=0)*

## Reduced dimension approaches: limitations

### Collisional excitation of $\text{HeH}^+$ by $\text{H}$

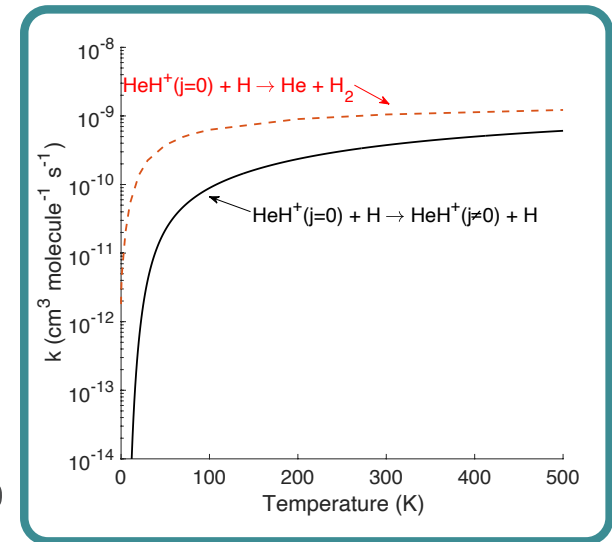
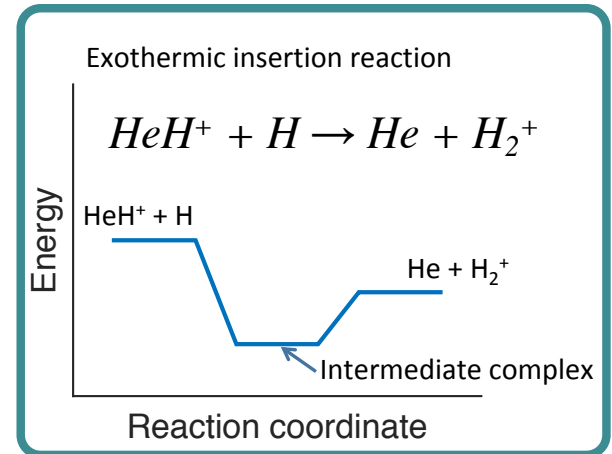
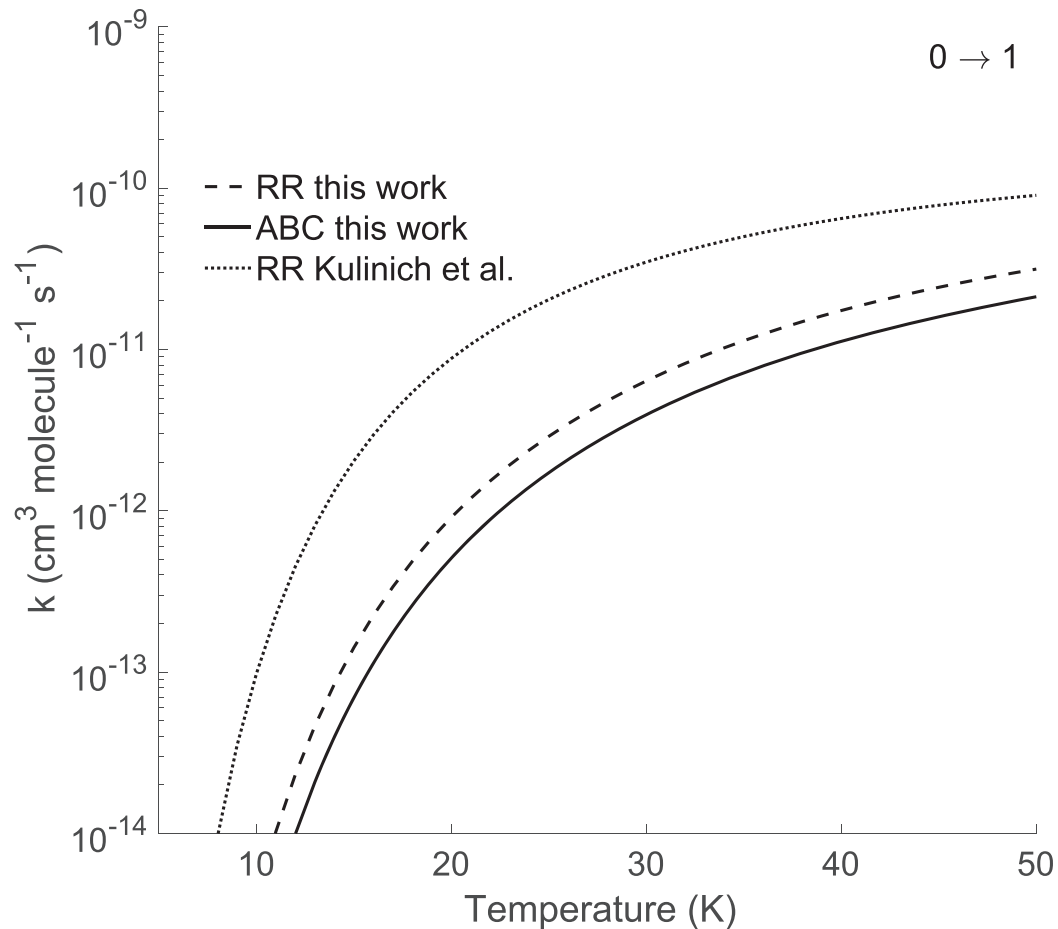


Rate coefficients for the rotational excitation of  $\text{HeH}^+$  ( $j = 0 \rightarrow j' = 1$ ) by  $\text{H}$ .  
— 3D reactive results; -- non reactive results; ... Kulinich et al. (2020)

- Rigid rotors calculations overestimate the exact reactive ones
- Need of a **method considering the competition between inelastic and reactive collisions**

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## Statistical approaches

**Statistical adiabatic channels model (SACM; Quack & Troe 1974, Loreau et al. 2018)**

**Statistical approach** - Adiabatic channels (*adiabats*) obtained by diagonalizing the Hamiltonian excluding the nuclear kinetic term for each  $J$ :

$$\langle \alpha' | H_{\text{int}} + V + \frac{\mathbf{L}^2}{2\mu R^2} | \alpha \rangle$$

$\alpha$  : angular functions of  $\Psi$

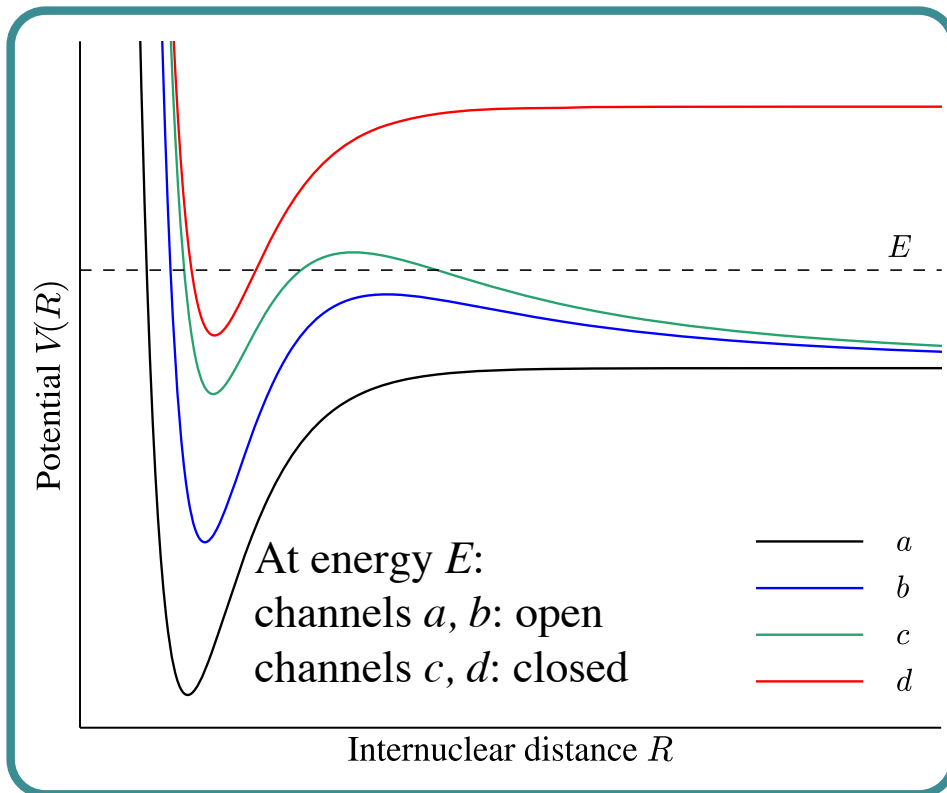
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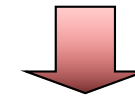
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We assume that all open channels have the same probability  $1/N(E, J)$ , where  $N(E, J)$  is the number of open channels at an energy  $E$  for a given  $J$ :

$$|S_{ij}(E, J)|^2 = \begin{cases} 1/N(E, J) & \text{for open channels} \\ 0 & \text{for closed channels} \end{cases}$$



$$\sigma_{if}(E) = \frac{\pi}{(2j_1 + 1)(2j_2 + 1)k^2} \sum_{J=0}^{\infty} (2J + 1) |S_{if}(E, J)|^2.$$



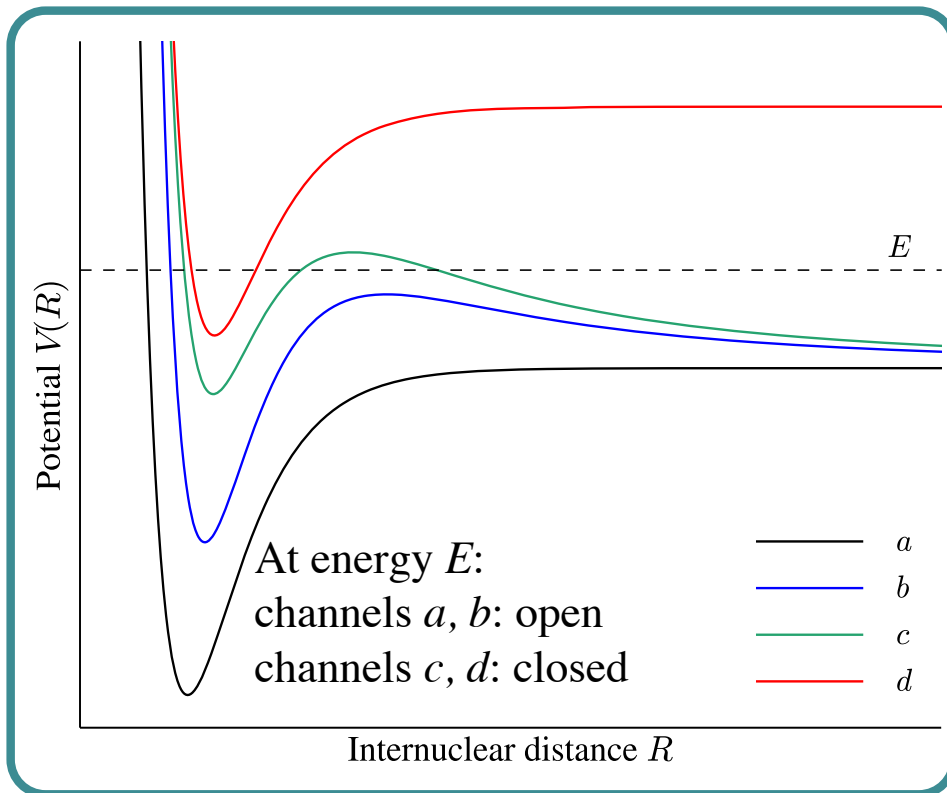
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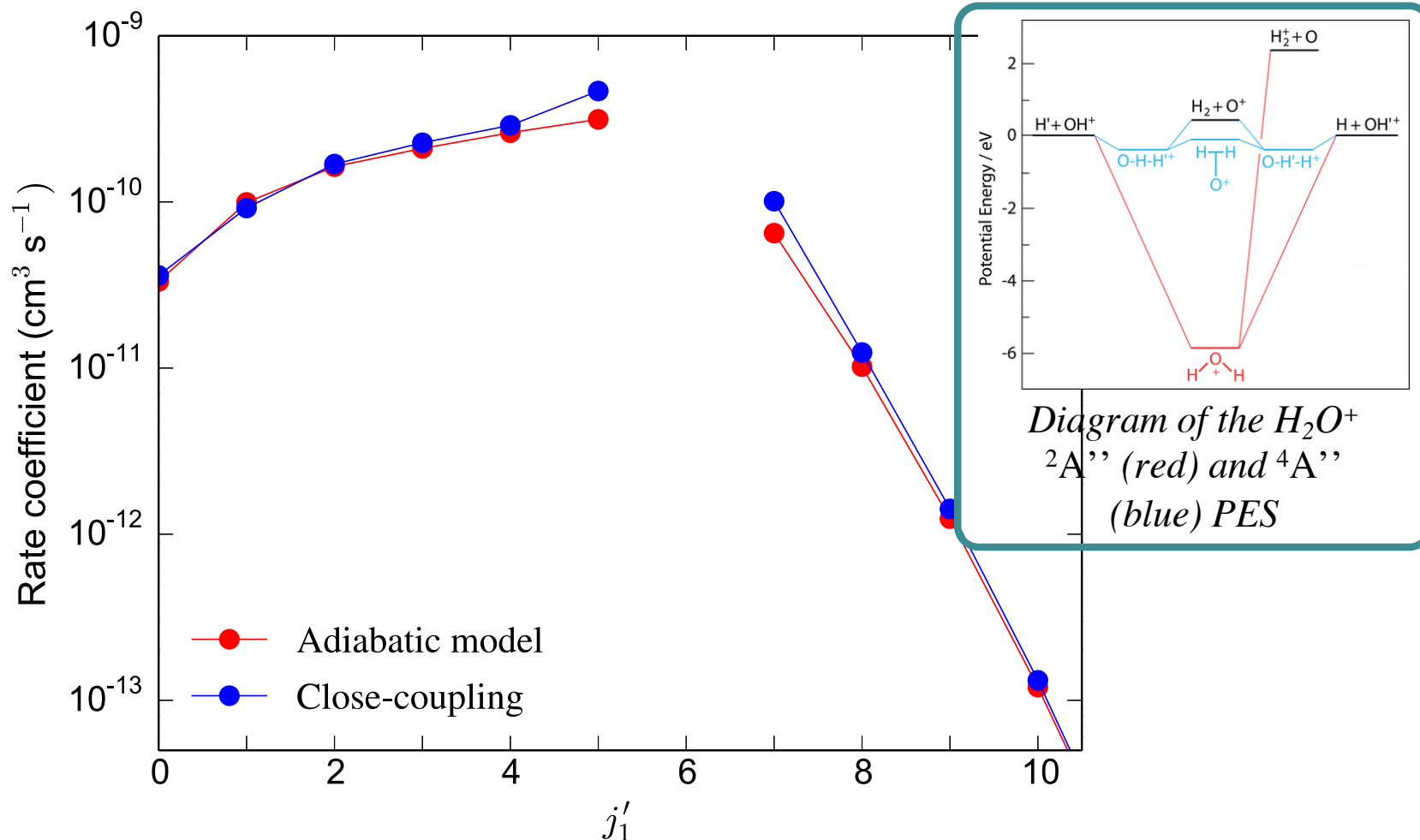
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- No need to include closed channels / The adiabatic curves are independent of energy
- Expected to be valid for collisional systems with a long-lived intermediate complex

## Statistical approaches OH<sup>+</sup>-H

### Application to the OH<sup>+</sup> - H strongly bound (non reactive) system

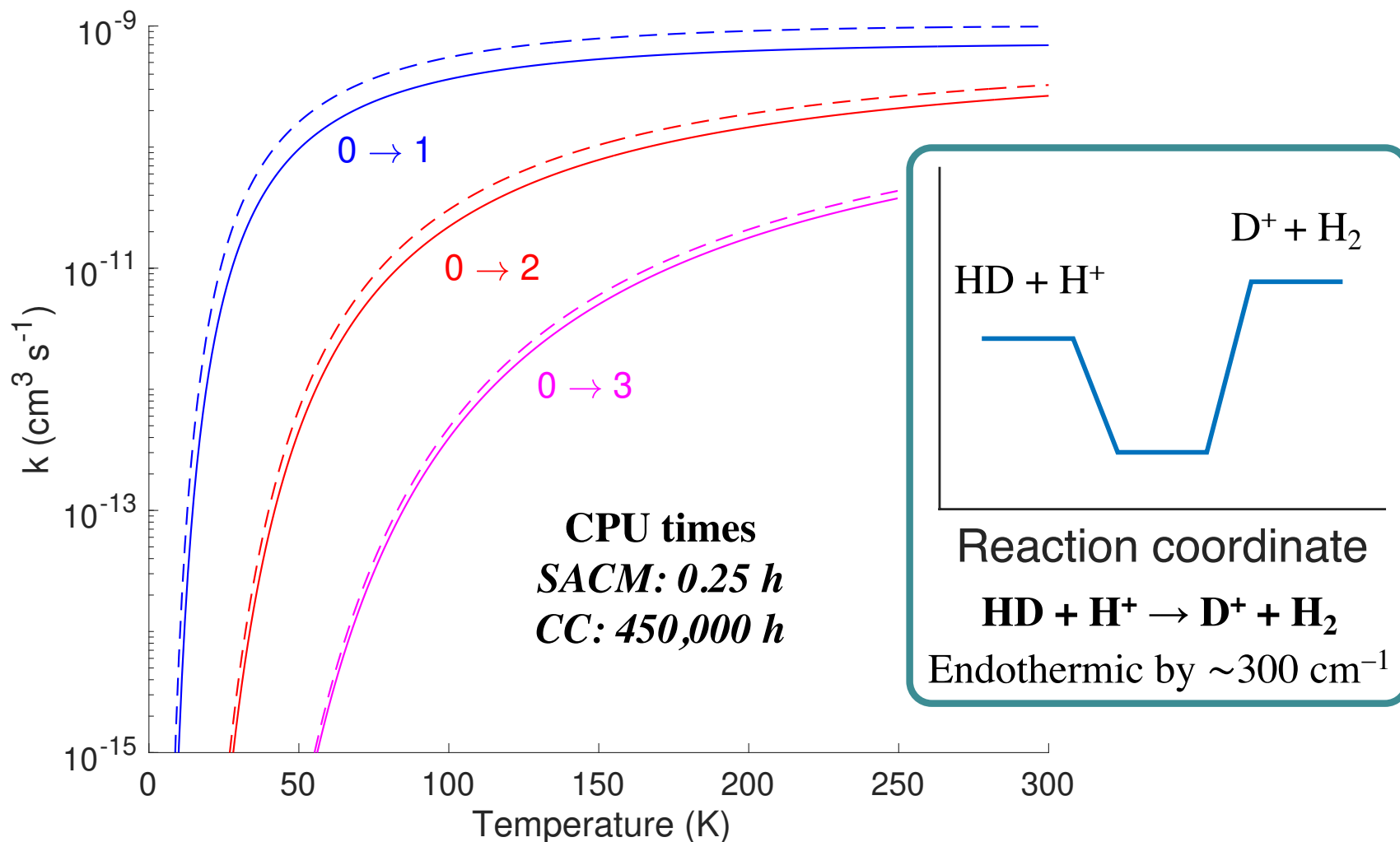


Rate coefficients for  $OH^+(j_1 = 6) + H \rightarrow OH^+(j_1) + H$  as a function of  $j_1'$  at a temperature of 200 K.

- The SACM approach slightly underestimates the transitions with  $\Delta j_1 = 1$  compared to the CC results, but all other transitions and **propensities are nicely reproduced**

## Statistical approaches: HD-H<sup>+</sup>

### Application to the HD - H<sup>+</sup> reactive system

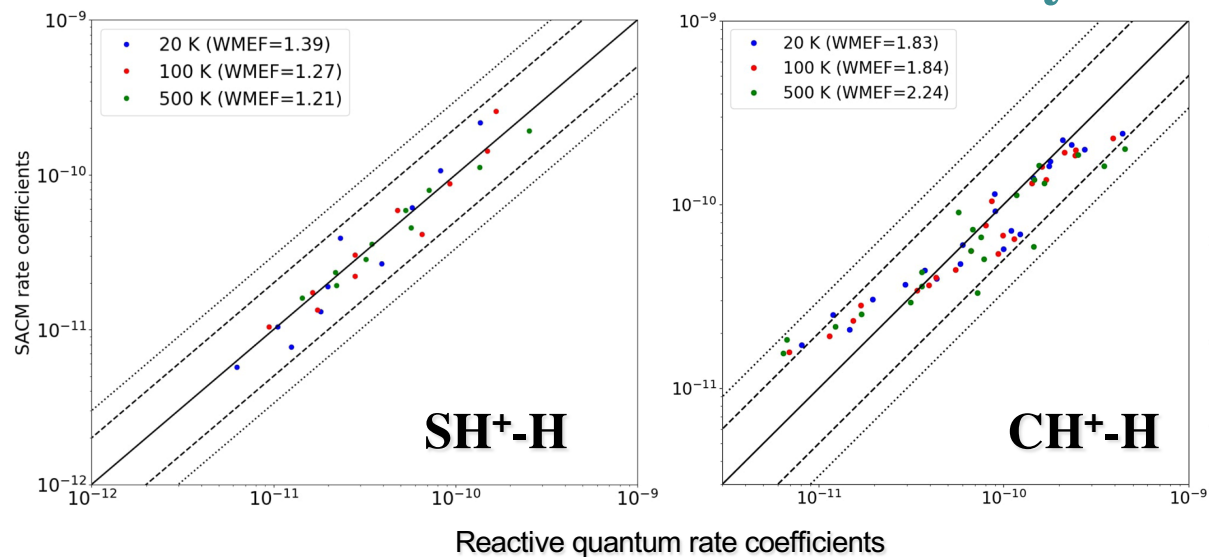


*Rate coefficients for the rotational excitation of HD by H<sup>+</sup>. CC (solid lines) vs. SACM (dashed lines)*

- The two sets of data are in **very good agreement**, with differences lower than a factor of 1.5

# Statistical approaches: applications

## Collisional excitation of SH<sup>+</sup> and CH<sup>+</sup> by H



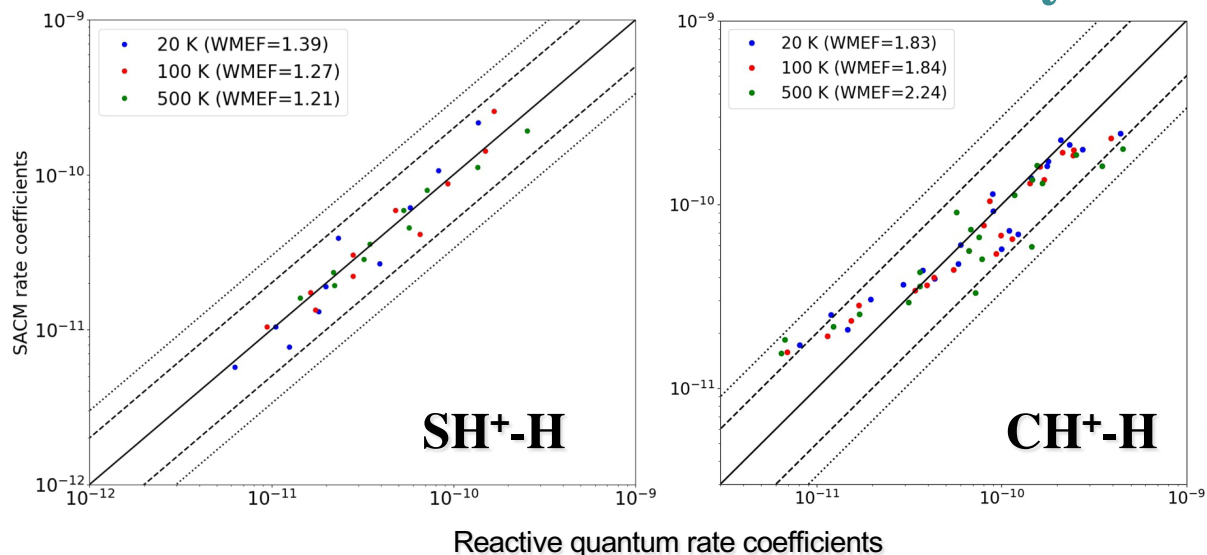
$$\text{WMEF} = \frac{\sum_i k_i^{\text{CC}} r_i}{\sum_i k_i^{\text{CC}}}$$

**SACM provides an interesting alternative to « almost » exact quantum calculations**

*Comparison at several temperatures of the SACM and the quantum rate coefficients*

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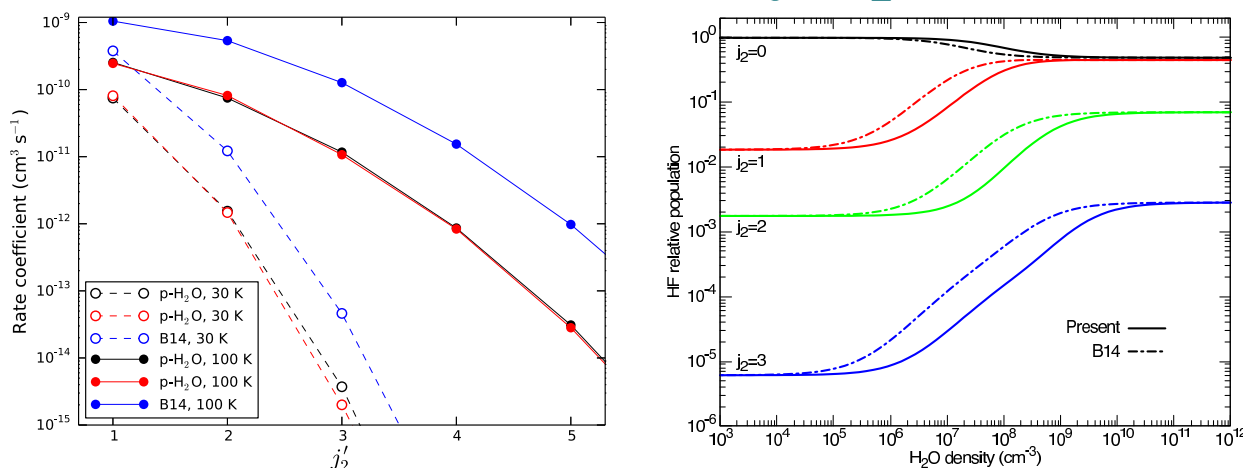


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## Collisional excitation of HF by H<sub>2</sub>O



**First state-to-state rate coefficients for the HF-H<sub>2</sub>O collisional system**

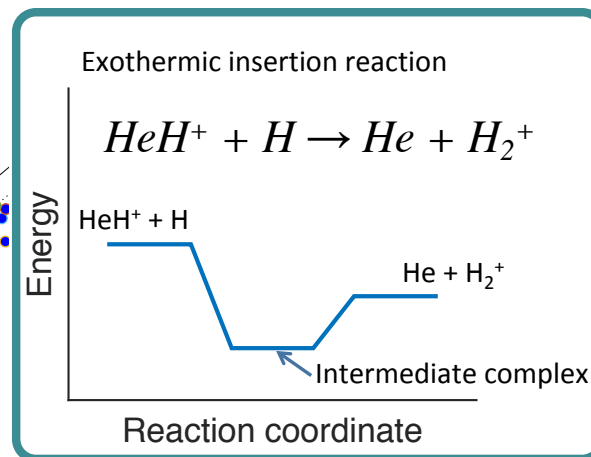
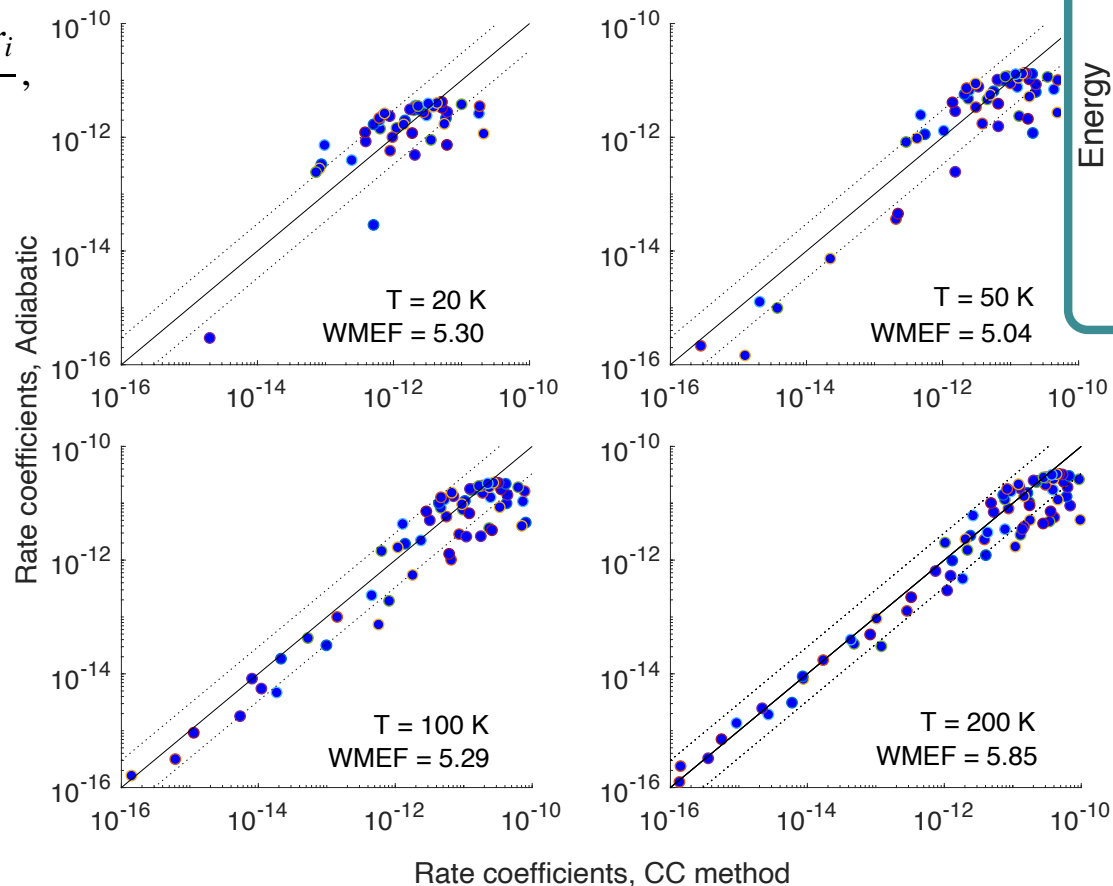
Left: Rate coefficients for the rotational excitation of HF (j<sub>2</sub>=0 – j<sub>2</sub>') by H<sub>2</sub>O

Right : Level populations of HF(j<sub>2</sub> = 0–3) as functions of H<sub>2</sub>O density in cometary comae model

# Statistical approaches: limitations

## Collisional excitation of HeH<sup>+</sup> by H

$$\text{WMEF} = \frac{\sum_i k_i^{\text{CC}} r_i}{\sum_i k_i^{\text{CC}}}$$



*SACM and CC rate coefficients for HeH<sup>+</sup>(j) + H collisions*

- SACM predicts the rate coefficients with a **reasonable accuracy**. Most rate coefficients are accurate to within a factor 2-3.
- Discrepancies attributed to a non favourable formation of the complex

## Conclusion

- **Production of new collisional data for ions and radicals** ( $\text{H}_3\text{O}^+$ ,  $\text{CF}^+$ ,  $\text{NS}^+$ ,  $\text{C}_2\text{H}$ ,  $\text{OH}$ )
- **Validation of the statistical adiabatic channels models** for scattering calculations at low temperatures and for strongly bound and reactive systems
- Ongoing work:  
*Generation of a SACM code to treat collisional excitation of ionic polyatomic systems*  
*Application to the  $\text{OH}^+$  and  $\text{H}_2\text{O}^+$  ions*
- Accurate **determination of the abundance of reactive molecules** in the interstellar medium



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**Thanks for your  
attention !**